

83 Kertaustehtäviä

Yhtälöitä ovat

$$\begin{aligned} 2x-1 &= 5y+8 \\ x:4 &= -11 \\ 31x &= 601 \\ 7(x+6) &= 0 \end{aligned}$$

Yhtäläisyysmerkki kahden lausekkeen välissä

881

$x=2$  sijoita yhtälöön, laske vasemman ja oikean puolet arvot

a)  $x-3=5$   
 $2-3=5$   
 $-1=5$

V: ei

b)  $3x+1=2x+3$   
 $3 \cdot 2+1=2 \cdot 2+3$   
 $6+1=4+3$   
 $7=7$

V: on

c)  $6-x=4$   
 $6-2=4$   
 $4=4$

V: on

d)  $2x+1=3$   
 $2 \cdot 2+1=3$   
 $4+1=3$   
 $5=3$

V: ei

882

a)  $x+2=5 \quad ||-2$   
 $x+2-2=5-2$   
 $x=3$

b)  $x-5=13 \quad ||+5$   
 $x-5+5=13+5$   
 $x=18$

c)  $x+11=17 \quad ||-11$   
 $x+11-11=17-11$   
 $x=6$

d)  $x-3=21 \quad ||+3$   
 $x-3+3=21+3$   
 $x=24$

883

a)  $2x=14 \quad ||:2$   
 $\frac{2x}{2} = \frac{14}{2}$   
 $x=7$

b)  $\frac{z}{3}=6 \quad || \cdot 3$   
 $\frac{3z}{3} = 3 \cdot 6$   
 $z=18$

c)  $\frac{y}{5}=1 \quad || \cdot 5$   
 $\frac{5y}{5} = 5 \cdot 1$   
 $y=5$

d)  $bx=3b \quad ||:b$   
 $\frac{bx}{b} = \frac{3b}{b}$   
 $x=b$

e)  $-5x=35 \quad ||:-5$   
 $\frac{-5x}{-5} = \frac{35}{-5}$   
 $x=-7$

f)  $\frac{x}{6}=-5 \quad || \cdot 6$   
 $\frac{6x}{6} = 6 \cdot (-5)$   
 $x=-30$

884

a)  $4x+5=3x \quad ||-3x$   
 $x+5=0 \quad ||-5$   
 $x=-5$

b)  $8x-5=7x \quad ||-7x$   
 $x-5=0 \quad ||+5$   
 $x=5$

c)  $5x+11=4x-2 \quad ||-4x$   
 $x+11=-2 \quad ||-11$   
 $x=-2-11$   
 $x=-13$

d)  $-x-8=-2x+1 \quad ||+2x$   
 $x-8=1 \quad ||+8$   
 $x=1+8$   
 $x=9$

$$885 \quad a) \quad \frac{4x}{3} = 12 \quad || \cdot 3$$

$$\frac{3 \cdot 4x}{3} = 3 \cdot 12$$

$$4x = 36 \quad || : 4$$

$$\frac{4x}{4} = \frac{36}{4}$$

$$x = 9$$

83 kertauslehtiä

$$b) \quad \frac{3x}{5} = -9 \quad || \cdot 5$$

$$\frac{5 \cdot 3x}{5} = 5 \cdot (-9)$$

$$3x = -45 \quad || : 3$$

$$\frac{3x}{3} = \frac{-45}{3}$$

$$x = -15$$

$$886 \quad a) \quad -3x - 5 = -8 \quad || + 5$$

$$-3x = -8 + 5$$

$$-3x = -3 \quad || : -3$$

$$\frac{-3x}{-3} = \frac{-3}{-3}$$

$$x = 1$$

$$b) \quad x - 3 = 3x + 5 \quad || - 3x$$

$$-2x - 3 = 5 \quad || + 3$$

$$-2x = 5 + 3 \quad || : -2$$

$$-2x = 8$$

$$\frac{-2x}{-2} = \frac{8}{-2}$$

$$x = -4$$

$$c) \quad \frac{x}{2} - 1 = 4 \quad || + 1$$

$$\frac{x}{2} = 5 \quad || \cdot 2$$

$$\frac{2x}{2} = 2 \cdot 5$$

$$x = 10$$

$$d) \quad 7 = -5x - 8 \quad || + 5x$$

$$5x + 7 = -8 \quad || - 7$$

$$5x = -8 - 7 \quad || : 5$$

$$5x = -15$$

$$\frac{5x}{5} = \frac{-15}{5}$$

$$x = -3$$

$$887 \quad a) \quad 6x = 0 \quad || : 6$$

$$\frac{6x}{6} = \frac{0}{6}$$

$$x = 0$$

$$b) \quad -x = 5 \quad || \cdot -1$$

$$x = -5$$

$$c) \quad 2x - 1 = 1 \quad || + 1$$

$$2x = 2 \quad || : 2$$

$$x = 1$$

$$d) \quad \frac{x}{8} = 0 \quad || \cdot 8$$

$$x = 0$$

$$888 \quad a) \quad 4x + 7 = 11 \quad || - 7$$

$$4x = 4 \quad || : 4$$

$$x = 1$$

$$b) \quad 4x + 7 = 19 \quad || - 7$$

$$4x = 12 \quad || : 4$$

$$x = 3$$

$$c) \quad 4x + 7 = -9 \quad || - 7$$

$$4x = -16 \quad || : 4$$

$$x = -4$$

$$889 \quad a) \quad x + 3 = -11 \quad || - 3$$

$$x = -11 - 3$$

$$x = -14$$

$$b) \quad 5 - x = 3 \quad || - 5$$

$$-x = -2 \quad || \cdot -1$$

$$x = 2$$

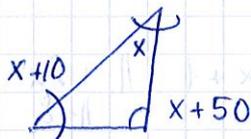
$$c) \quad x \cdot 7 = 3x + 8 \quad || - 3x$$

$$7x = 3x + 8 \quad || : 4$$

$$4x = 8$$

$$x = 2$$

890



Kulmat ovat  $x$ ,  $x+10$  ja  $x+50$

Niiden summa on  $180^\circ$

$$x + x + 10 + x + 50 = 180$$

$$3x + 60 = 180 \quad || - 60$$

$$3x = 120 \quad || : 3$$

$$x = 40$$

V:

Kulmat ovat

$$x = 40^\circ$$

$$x + 10 = 50^\circ$$

$$x + 50 = 90^\circ$$

Harjoittele  
S.176

### 88 Kertavastetäviä

891

Norppa + halli 400 kg

Norppa  $x$

Halli  $3x$

$$3x + x = 400$$

$$4x = 400$$

$$x = 100$$

||:4

(Norppa)

$$3x = 3 \cdot 100 = 300$$

(Halli)

V: Norppa 100 kg, halli 300 kg

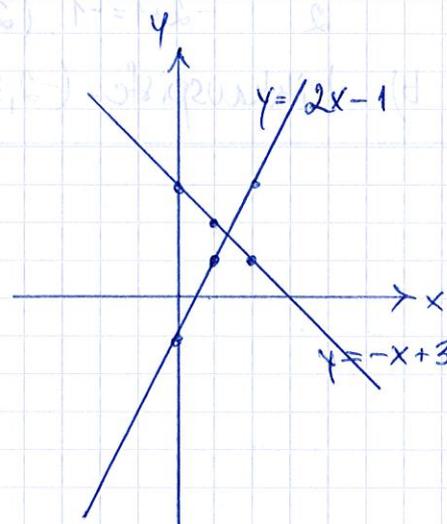
892

a)  $y = 2x - 1$

x	$y = 2x - 1$	(x, y)
0	$2 \cdot 0 - 1 = -1$	(0, -1)
1	$2 \cdot 1 - 1 = 1$	(1, 1)
2	$2 \cdot 2 - 1 = 3$	(2, 3)

$$y = -x + 3$$

x	$y = -x + 3$	(x, y)
0	$-0 + 3 = 3$	(0, 3)
1	$-1 + 3 = 2$	(1, 2)
2	$-2 + 3 = 1$	(2, 1)



893

a) (1, 5)

$$y = 2x + 3$$

$$5 = 2 \cdot 1 + 3$$

$$5 = 2 + 3$$

$$5 = 5$$

V: on

b) (2, 7)

$$y = 2x + 3$$

$$7 = 2 \cdot 2 + 3$$

$$7 = 4 + 3$$

$$7 = 7$$

V: on

b) (-3, -3)

$$y = 2x + 3$$

$$-3 = 2 \cdot (-3) + 3$$

$$-3 = -6 + 3$$

$$-3 = -3$$

V: on

894

$$y = -2x + 7$$

x	$y = -2x + 7$	(x, y)
0	$-2 \cdot 0 + 7 = 7$	(0, 7)
1	$-2 \cdot 1 + 7 = 5$	(1, 5)
2	$-2 \cdot 2 + 7 = 3$	(2, 3)

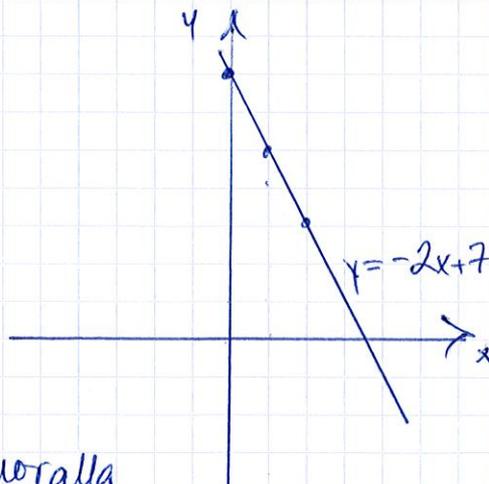
(35, -77)

b)  $-77 = -2 \cdot 35 + 7$

$$-77 = -70 + 7$$

$$-77 = -63$$

V: ei ole suoralla



harjoittele  
s.176

83 kertaus tehtäviä

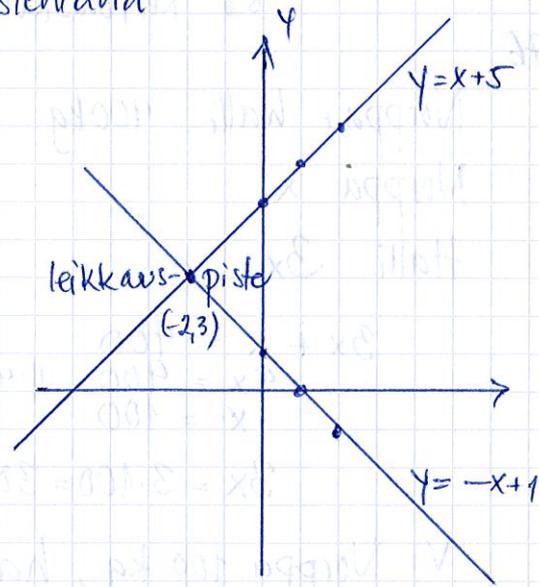
895 a)  $y = x + 5$

x	$y = x + 5$	(x, y)
0	$0 + 5 = 5$	(0, 5)
1	$1 + 5 = 6$	(1, 6)
2	$2 + 5 = 7$	(2, 7)

$y = -x + 1$

x	$y = -x + 1$	(x, y)
0	$-0 + 1 = 1$	(0, 1)
1	$-1 + 1 = 0$	(1, 0)
2	$-2 + 1 = -1$	(2, -1)

b) leikkauspiste (-2, 3)



$x <$   
 $y = -x + 1$

(x, y)	$y = -x + 1$	x
(-1, 0)	$-(-1) + 1 = 2$	0
(0, 1)	$-0 + 1 = 1$	1
(1, 0)	$-1 + 1 = 0$	0
(2, -1)	$-2 + 1 = -1$	1

(x, y)	$y = x + 5$	x
(-2, 3)	$-2 + 5 = 3$	3
(-1, 4)	$-1 + 5 = 4$	4
(0, 5)	$0 + 5 = 5$	5
(1, 6)	$1 + 5 = 6$	6
(2, 7)	$2 + 5 = 7$	7

(x, y)	$y = -x + 1$	x
(-2, 3)	$-(-2) + 1 = 3$	3
(-1, 2)	$-(-1) + 1 = 2$	2
(0, 1)	$-0 + 1 = 1$	1
(1, 0)	$-1 + 1 = 0$	0
(2, -1)	$-2 + 1 = -1$	-1

(x, y)	$y = x + 5$	x
(-2, 3)	$-2 + 5 = 3$	3
(-1, 4)	$-1 + 5 = 4$	4
(0, 5)	$0 + 5 = 5$	5
(1, 6)	$1 + 5 = 6$	6
(2, 7)	$2 + 5 = 7$	7

$x <$   
 $y = x + 5$

(x, y)	$y = -x + 1$	x
(-2, 3)	$-(-2) + 1 = 3$	3
(-1, 2)	$-(-1) + 1 = 2$	2
(0, 1)	$-0 + 1 = 1$	1
(1, 0)	$-1 + 1 = 0$	0
(2, -1)	$-2 + 1 = -1$	-1

$x <$   
 $y = x + 5$

896

$$\begin{aligned} a) \quad x-9 &= 13-x & ||+x \\ 2x-9 &= 13 & ||+9 \\ 2x &= 22 & ||:2 \\ x &= 11 \end{aligned}$$

$$\begin{aligned} b) \quad 11-x &= 26 & ||-11 \\ -x &= 15 & ||\cdot-1 \\ x &= -15 \end{aligned}$$

$$\begin{aligned} c) \quad 4x+17 &= 5x-56 & ||-5x \\ -x+17 &= -56 & ||-17 \\ -x &= -56-17 & \\ -x &= -73 & ||\cdot-1 \\ x &= 73 \end{aligned}$$

$$\begin{aligned} d) \quad 3x-52 &= 18-4x & ||+4x \\ 7x-52 &= 18 & ||+52 \\ 7x &= 70 & ||:7 \\ x &= 10 \end{aligned}$$

897

Muodostetaan lausekkeista yhtälö

$$\begin{aligned} 2x-8 &= 5x+1 & ||-5x \\ -3x-8 &= 1 & ||+8 \\ -3x &= 9 & ||:-3 \\ -3x &= 9 & \\ -3 &= 3 & \\ x &= -3 \end{aligned}$$

898

$$\begin{aligned} a) \quad 3x-8 &= 12-x & ||+x \\ 4x-8 &= 12 & ||+8 \\ 4x &= 20 & ||:4 \\ x &= 5 \end{aligned}$$

$$\begin{aligned} b) \quad \frac{x}{5} + 1 &= 7 & ||-1 \\ \frac{x}{5} &= 6 & ||\cdot 5 \\ \frac{5x}{5} &= 5\cdot 6 & \\ x &= 30 \end{aligned}$$

899



kantakulmat  $x$   
huippukulma  $x+30$

Kolmion kulmien summa  $180^\circ$

$$x + x + x + 30 = 180$$

$$3x + 30 = 180 \quad ||-30$$

$$3x = 150 \quad ||:3$$

$$x = 50 \quad (\text{kantakulma})$$

$$x+30 = 50+30 = 80 \quad (\text{huippukulma})$$

$$V: 50^\circ, 50^\circ \text{ ja } 80^\circ$$

900

Kokonaisluvut ovat  $x$  ja  $x+1$   
Niiden summa 119

$$x + x + 1 = 119$$

$$2x + 1 = 119 \quad ||-1$$

$$2x = 118 \quad ||:2$$

$$x = 118 : 2 = 59 \quad x+1 = 59+1 = 60$$

$$V: 59 \text{ ja } 60$$

903	Nuorimmainen saldo	Keskimmäinen saldo	Vanhin saldo	Yht.
Huom! järjestys vaihtui	$x$	$x+4$	$x+4+6$	50

$$x + x + 4 + x + 10 = 50$$

$$3x + 14 = 50 \quad || -14$$

$$3x = 36 \quad || :3$$

$$x = 12$$

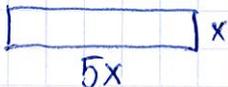
(nuorin)

$$x + 4 = 12 + 4 = 16 \quad (\text{kesk.})$$

$$x + 10 = 12 + 10 = 22 \quad (\text{vanhin})$$

V: nuoria 12 €, keskimäinen 16 € ja vanhin 22 €

901



piiri 228 cm

$$2 \cdot x + 2 \cdot 5x = 228$$

$$2x + 10x = 228$$

$$12x = 228 \quad || :12$$

$$x = \frac{228}{12}$$

$$x = 19 \quad (\text{korkeus})$$

$$5x = 5 \cdot 19 = 95 \quad (\text{kanta})$$

V: kanta 95 cm, korkeus 19 cm

902

Pyöriäisiä	Norppia	Halleja	Yht.
$x$	$20x$	$20x + 3000$	23500

$$x + 20x + 20x + 3000 = 23500$$

$$41x + 3000 = 23500 \quad || -3000$$

$$41x = 20500 \quad || :41$$

$$x = 20500 : 41$$

$$x = 500$$

(pyör.)

$$20x = 20 \cdot 500 = 10000 \quad (\text{norppia})$$

$$20x + 3000 = 10000 + 3000 \quad (\text{halleja})$$

$$= 13000$$

V: 500 pyöriäistä, 10000 norppaa ja 13000 hallia

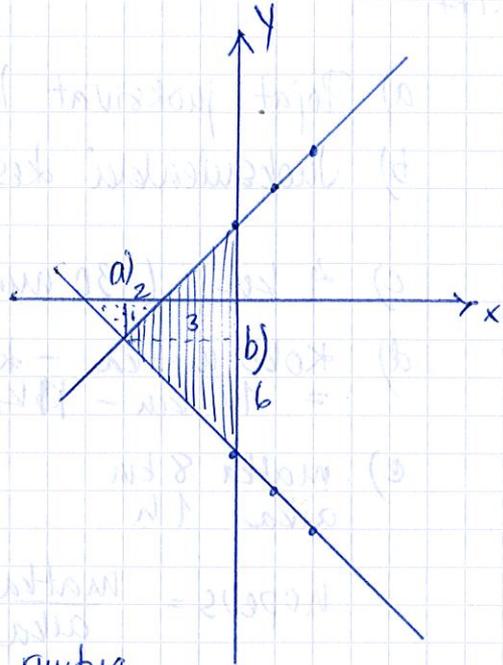
904

$$y = x + 2$$

x	y = x + 2	(x, y)
0	0 + 2 = 2	(0, 2)
1	1 + 2 = 3	(1, 3)
2	2 + 2 = 4	(2, 4)

$$y = -x - 4$$

x	y = -x - 4	(x, y)
0	-0 - 4 = -4	(0, -4)
1	-1 - 4 = -5	(1, -5)
2	-2 - 4 = -6	(2, -6)



a)  $A = \frac{\text{kanta} \cdot \text{korkeus}}{2} = \frac{2 \cdot 3}{2} = 1$  ruutua

b)  $A = \frac{\text{kanta} \cdot \text{korkeus}}{2} = \frac{6 \cdot 3}{2} = 9$  ruutua

905

a) A(5, □) on suoralla  $y = 3x - 7$   
sijoitetaan  $x = 5$  yhtälöön, ja lasketaan y:n arvo

$$y = 3 \cdot 5 - 7 = 15 - 7 = 8$$

V: y = 8

b) B(-5, □)

$$y = 3 \cdot (-5) - 7 = -15 - 7 = -22$$

V: y = -22

c) C(□, 32)

Sijoitetaan  $y = 32$  suoran yhtälöön ja ratkaistaan x.

$$32 = 3x - 7 \quad || +7$$

$$39 = 3x$$

$$3x = 39 \quad || :3$$

$$x = 13$$

V: x = 13

d) D(□, -40)

$$-40 = 3x - 7 \quad || +7$$

$$-33 = 3x \quad || :3$$

$$-11 = x$$

V: x = -11

906

a) Pojat juoksivat 14 km

b) Juoksulenkei kesti  $11.30 - 9.00 = 2.30$   
2 h 30 min

c) 4 km (30 min vastaava y-koordinaatti on 4)

d) Koko matka - kuljettu matka klo 11  
 $= 14 \text{ km} - 11 \text{ km} = \underline{3 \text{ km}}$

e) matka 8 km  
aika 1 h

$$\text{nopeus} = \frac{\text{matka}}{\text{aika}} = \frac{8 \text{ km}}{1 \text{ h}} = 8 \text{ km/h}$$

f) matka  $14 \text{ km} - 8 \text{ km} = 6 \text{ km}$   
aika 1 h

$$\text{nopeus} = \frac{\text{matka}}{\text{aika}} = \frac{6 \text{ km}}{1 \text{ h}} = 6 \text{ km/h}$$